Probabilistic Operator Algebra Seminar

Organizer: Dan-Virgil Voiculescu

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Title: Modular Structure and Inclusions of Twisted Araki-Woods Algebras.

In the general setting of twisted second quantization (including Bose/Fermi second quantization, Ssymmetric Fock spaces, and full Fock from free probability as special cases), von Neumann algebras on twisted Fock spaces are analyzed. These von Neumann algebras L(T, H) are called twisted Araki-Woods algebras and depend on a selfadjoint twist operator T and a standard subspace Hof the single particle Hilbert space. In this talk I will explain how the braid equation for T and an abstract version of the crossing symmetry from scattering theory encode for which L(T, H) the Fock vacuum is a cyclic and separating vector, and what the corresponding modular data are. I will then consider two types of inclusions of twisted Araki-Woods algebras generated by inclusions $K \subset H$ of standard subspaces. If the inclusion is half-sided modular and the twist satisfies a norm bound, $L(T, K) \subset L(T, H)$ is shown to be singular. If the inclusion $K \subset H$ satisfies a nuclearity condition, $L(T, K) \subset L(T, H)$ has type III relative commutant for suitable twists T.

This is joint work with Ricardo Correa da Silva (arXiv: 2212.02298)